

# Phase Rolling and the Impacts on Protection

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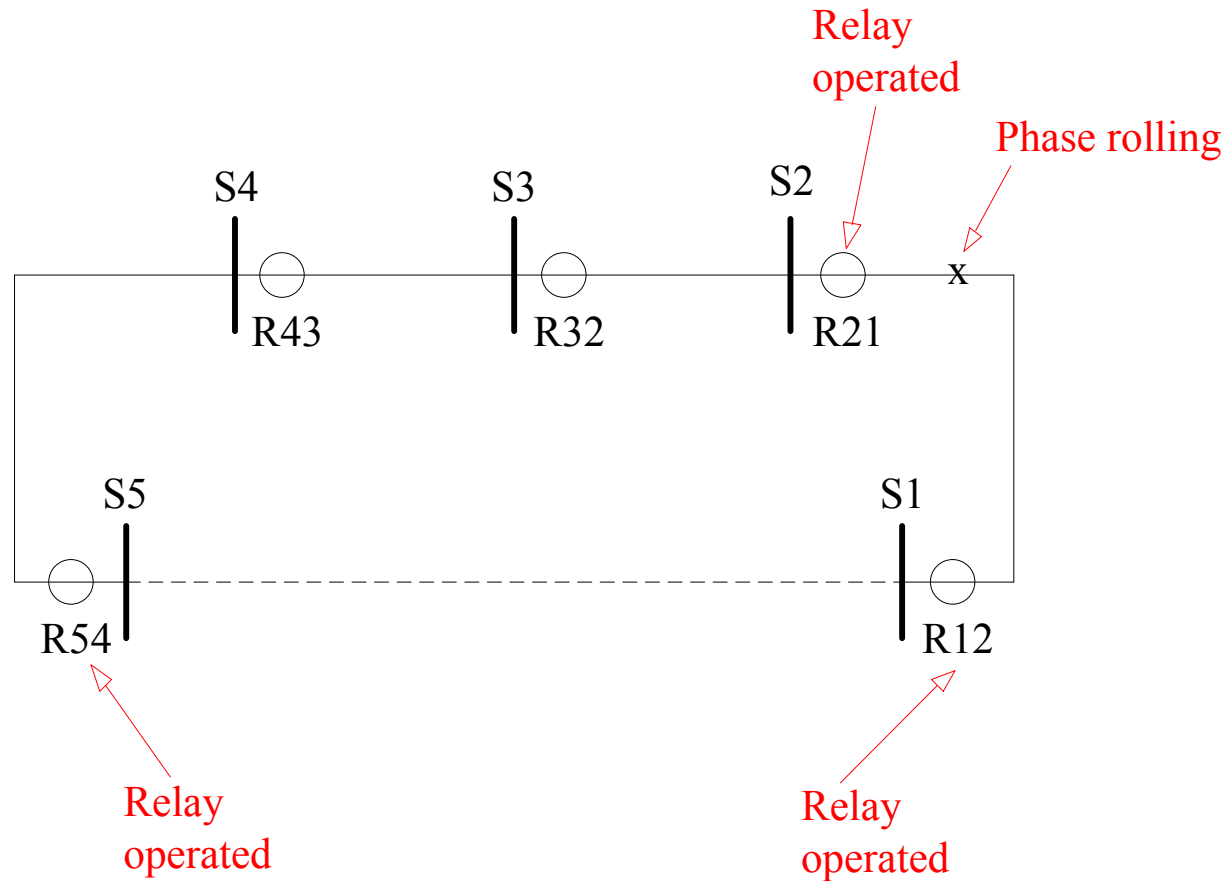
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# Overview

- ▶ Background Introduction.
- ▶ Relays Settings and Operation.
- ▶ Phase Rolling Characteristics.
- ▶ Solving the Currents for Phase Rolling.
- ▶ Sample calculation.
- ▶ Further Discussion.

# Introduction



# Questions

- ▶ Why did the under-reaching zone 1 distance element which is several buses away operate?
- ▶ Is there any way to prevent such situation beforehand?

# Relay Settings and the Measurements

Line impedance:  $4.97\Omega\angle 82.96^\circ$

Zone 1 reach:  $4.2\Omega\angle 82.96^\circ$

85% reaching

Measured voltage:  $V_b = 49.5\text{kV}\angle 318.4^\circ$ ,  $V_c = 48.4\text{kV}\angle 245.9^\circ$

Measured current:  $I_b = 7723.9\text{A}\angle 290.9^\circ$ ,  $I_c = 7618.0\angle 111.9^\circ$

All Data in  
Primary  
Side

# Relay Operation

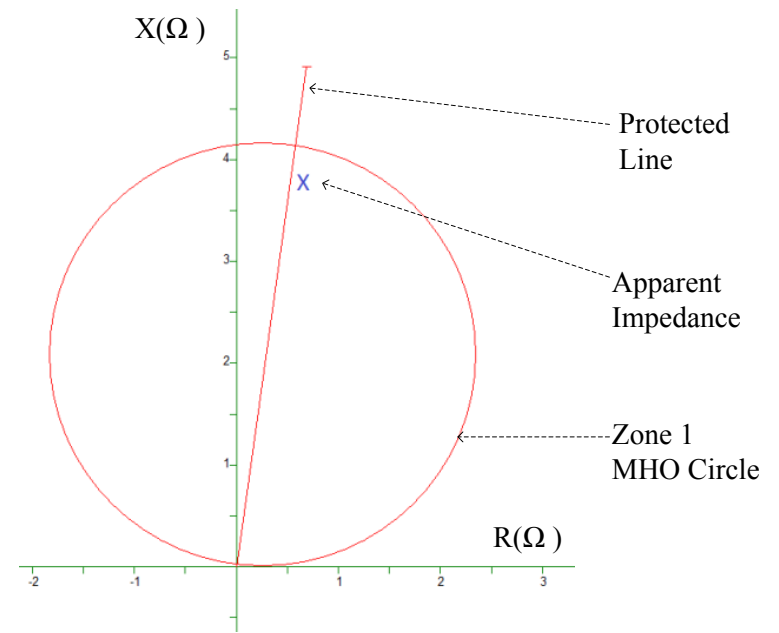
- Phase distance element impedance measurements

$$\begin{bmatrix} Z_{AB} \\ Z_{BC} \\ Z_{CA} \end{bmatrix} = \begin{bmatrix} \frac{V_A - V_B}{I_A - I_B} \\ \frac{V_B - V_C}{I_B - I_C} \\ \frac{V_C - V_A}{I_C - I_A} \end{bmatrix} \quad (1)$$

$$V_{bc} = 49.5\text{kV}\angle 318.4^\circ - 48.4\text{kV}\angle 245.9^\circ = 57.9\text{kV}\angle 11.3^\circ$$

$$I_{bc} = 7723.9\text{A}\angle 290.9^\circ - 7618.0\text{A}\angle 111.9^\circ = 15341.3\text{A}\angle -68.6^\circ$$

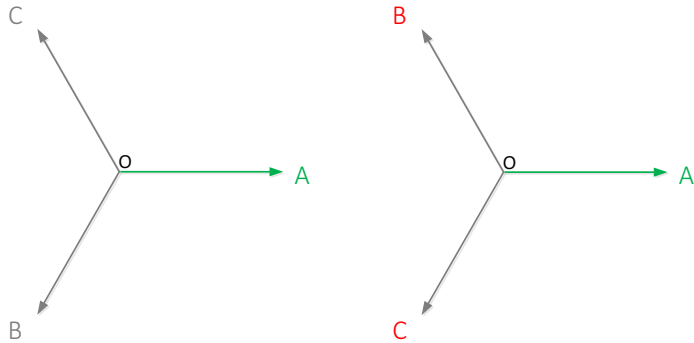
$$Z_{bc} = V_{bc} / I_{bc} = 57.9\text{kV}\angle 11.3^\circ / 15341.3\text{A}\angle -68.6^\circ = 3.77\Omega\angle 79.9^\circ$$



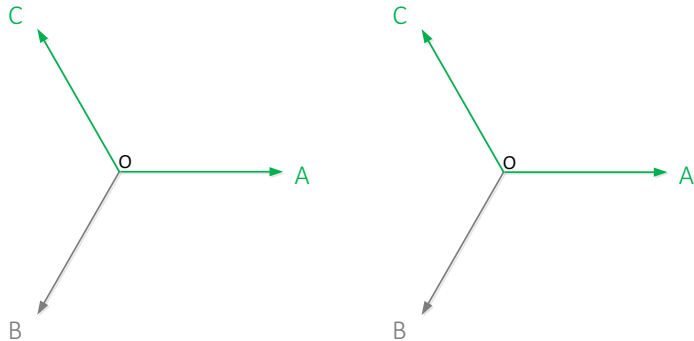
# Measures to Prevent Phase Rolling

- ▶ Phasing verification during commissioning time.
  - ❖ Simple and easy
  - ❖ Has been applied so far
- ▶ Special synchronizing scheme to prevent phase rolling closing.
  - ❖ Traditional synchronizing scheme doesn't solve the issue
  - ❖ Special scheme is possible to be developed
- ▶ Treatment of distance elements is challenging.
  - ❖ Could be complicate and challenging
  - ❖ Not recommended now that there are easy and simple solutions.

# Special Synchronizing Scheme



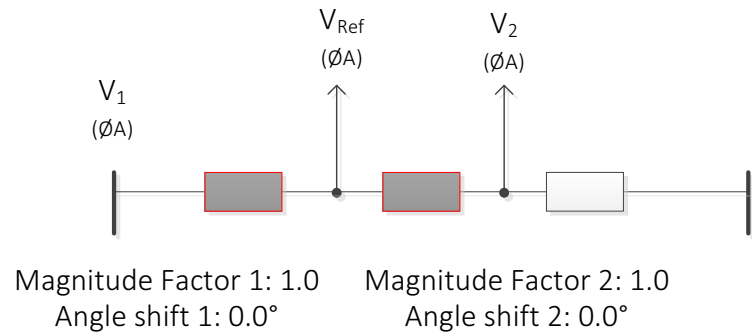
- ▶ Traditional phase synchronizing.
  - ❖ Phase A synchronized
  - ❖ Still possible to close with phase rolling



- ▶ Special synchronizing scheme.
  - ❖ Need to have 2 phases synchronized

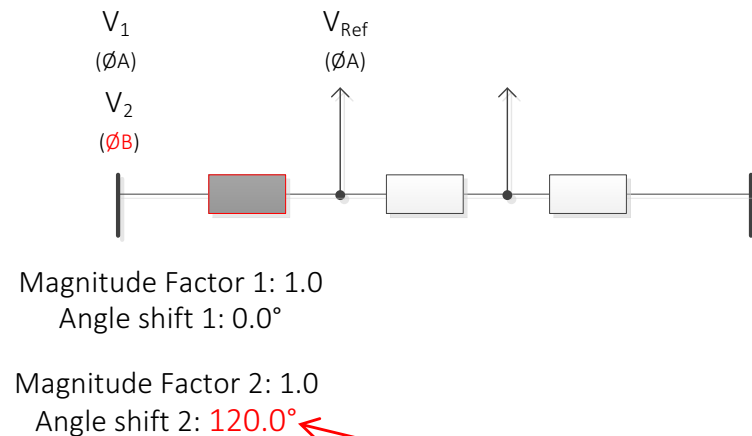


# Special Synchronizing Scheme (Cont'd)



## ▶ Typical 2 breaker synchronizing .

- ❖ Phase A synchronized
- ❖ Still possible to close with phase rolling



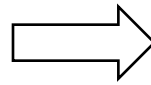
## ▶ Special synchronizing scheme.

- ❖ Need to have 2 phases synchronized
- ❖ Both V1 and V2 synchronized to close

Depending on the phase rotation  
ABC or ACB, angle shift could be  
either 120° or -120°

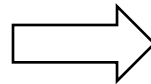
# Phase Rolling Characteristics

Rare Phenomenon

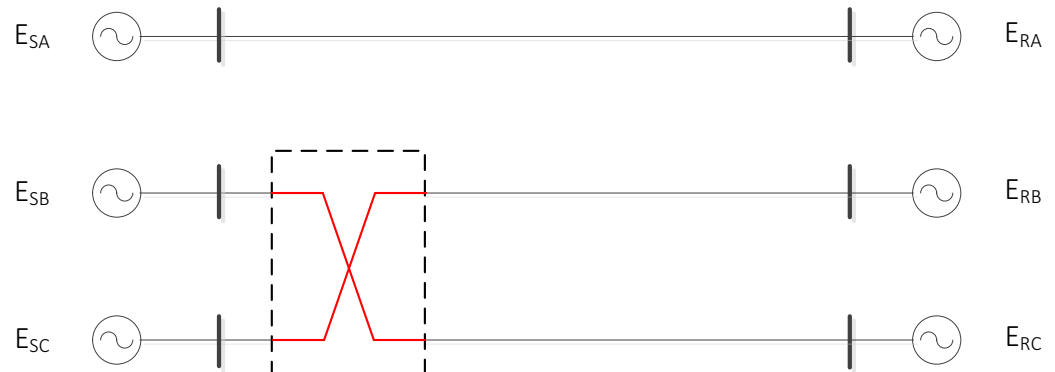


Regular Software  
Tool not Applicable

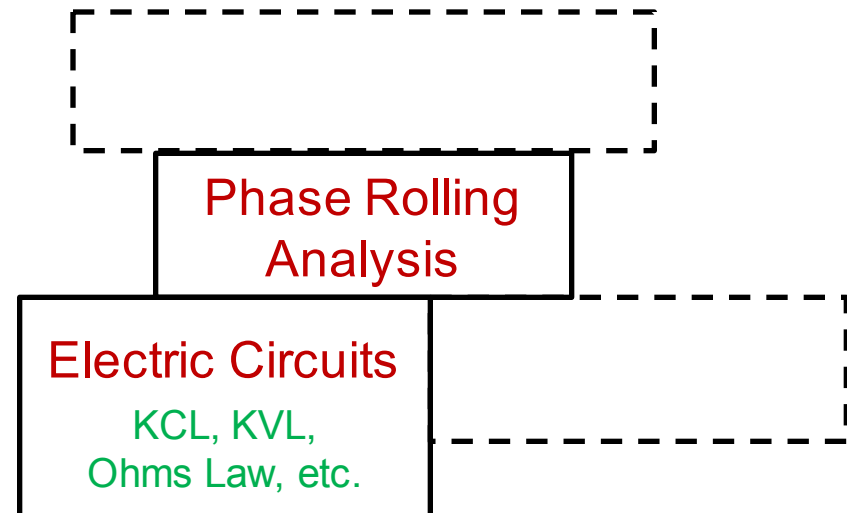
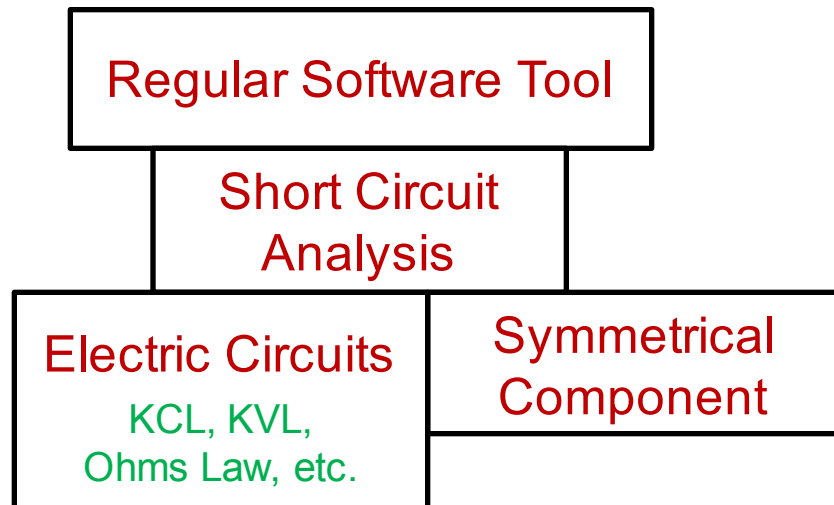
No Specific Location



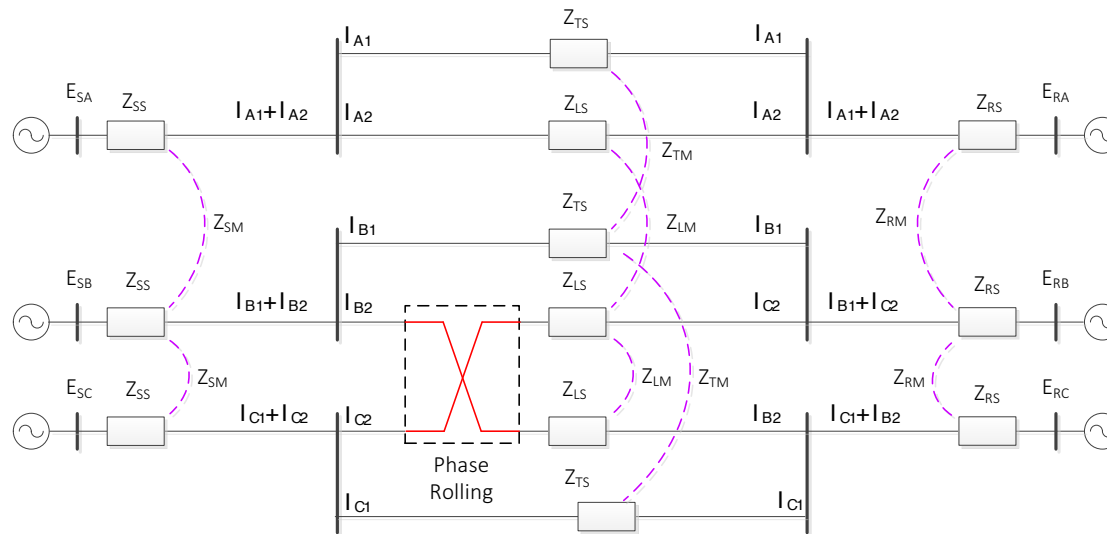
Apparent Impedance  
Relay – Fault Location  
Relay – System Configuration ←



# Analysis Method Compare



# Solving the Phase Rolling

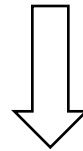


(Mutual are shown for phase A-B & B-C only for simplicity)

- $E_{SA}, E_{SB}, E_{SC}$  – Equivalent source potential
- $E_{RA}, E_{RB}, E_{RC}$  – Remote equivalent source potential
- $Z_{SS}, Z_{RS}$  – Equivalent self-impedances behind the relay and behind the remote terminal
- $Z_{SM}, Z_{RM}$  – Equivalent mutual impedances between phases behind the relay and behind the remote terminal
- $Z_{LS}, Z_{TS}$  – Subject line and transfer self-impedances
- $Z_{LM}, Z_{TM}$  – Subject line and transfer mutual impedances between phases
- $I_{A1}, I_{B1}, I_{C1}$  – Currents through the transfer impedances
- $I_{A2}, I_{B2}, I_{C2}$  – Currents through the subject relay (phase designation swapped at remote terminal)

# System Data (Impedances) Preparation

System Equivalence  
(By Regular Software Tools)



Sequence to Phase

$$Z_S = (Z_0 + 2Z_1)/3$$

$$Z_M = (Z_0 - Z_1)/3$$

Where,

$Z_S, Z_M$  – Self and mutual impedances

$Z_1, Z_0$  – Positive and zero sequence impedances

# Polynomials

$$Z_{SS}*(I_{A1}+I_{A2}) + Z_{SM}*(I_{B1}+I_{B2}+I_{C1}+I_{C2}) + Z_{TS}*I_{A1} + Z_{TM}*(I_{B1}+I_{C1}) + Z_{RS}*(I_{A1}+I_{A2}) + Z_{RM}*(I_{B1}+I_{B2}+I_{C1}+I_{C2}) = E_{SA}-E_{RA}$$

$$Z_{SS}*(I_{A1}+I_{A2}) + Z_{SM}*(I_{B1}+I_{B2}+I_{C1}+I_{C2}) + Z_{LS}*I_{A2} + Z_{LM}*(I_{B2}+I_{C2}) + Z_{RS}*(I_{A1}+I_{A2}) + Z_{RM}*(I_{B1}+I_{B2}+I_{C1}+I_{C2}) = E_{SA}-E_{RA}$$

$$Z_{SS}*(I_{B1}+I_{B2}) + Z_{SM}*(I_{A1}+I_{A2}+I_{C1}+I_{C2}) + Z_{TS}*I_{B1} + Z_{TM}*(I_{A1}+I_{C1}) + Z_{RS}*(I_{B1}+I_{C2}) + Z_{RM}*(I_{A1}+I_{A2}+I_{C1}+I_{B2}) = E_{SB}-E_{RB}$$

$$Z_{SS}*(I_{B1}+I_{B2}) + Z_{SM}*(I_{A1}+I_{A2}+I_{C1}+I_{C2}) + Z_{LS}*I_{B2} + Z_{LM}*(I_{A2}+I_{C2}) + Z_{RS}*(I_{C1}+I_{B2}) + Z_{RM}*(I_{A1}+I_{A2}+I_{B1}+I_{C2}) = E_{SB}-E_{RC}$$

$$Z_{SS}*(I_{C1}+I_{C2}) + Z_{SM}*(I_{A1}+I_{A2}+I_{B1}+I_{B2}) + Z_{LS}*I_{C2} + Z_{LM}*(I_{A2}+I_{B2}) + Z_{RS}*(I_{B1}+I_{C2}) + Z_{RM}*(I_{A1}+I_{A2}+I_{C1}+I_{B2}) = E_{SC}-E_{RB}$$

$$Z_{SS}*(I_{C1}+I_{C2}) + Z_{SM}*(I_{A1}+I_{A2}+I_{B1}+I_{B2}) + Z_{TS}*I_{C1} + Z_{TM}*(I_{A1}+I_{B1}) + Z_{RS}*(I_{C1}+I_{B2}) + Z_{RM}*(I_{A1}+I_{A2}+I_{B1}+I_{C2}) = E_{SC}-E_{RC}$$


Re-arrange

$$(Z_{SS}+Z_{TS}+Z_{RS})*I_{A1} + (Z_{SS}+Z_{RS})*I_{A2} + (Z_{SM}+Z_{TM}+Z_{RM})*I_{B1} + (Z_{SM}+Z_{RM})*I_{B2} + (Z_{SM}+Z_{TM}+Z_{RM})*I_{C1} + (Z_{SM}+Z_{RM})*I_{C2} = E_{SA}-E_{RA}$$

$$(Z_{SS}+Z_{RS})*I_{A1} + (Z_{SS}+Z_{LS}+Z_{RS})*I_{A2} + (Z_{SM}+Z_{RM})*I_{B1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{B2} + (Z_{SM}+Z_{RM})*I_{C1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{C2} = E_{SA}-E_{RA}$$

$$(Z_{SM}+Z_{TM}+Z_{RM})*I_{A1} + (Z_{SM}+Z_{RM})*I_{A2} + (Z_{SS}+Z_{TS}+Z_{RS})*I_{B1} + (Z_{SS}+Z_{RM})*I_{B2} + (Z_{SM}+Z_{TM}+Z_{RM})*I_{C1} + (Z_{SM}+Z_{RS})*I_{C2} = E_{SB}-E_{RB}$$

$$(Z_{SM}+Z_{RM})*I_{A1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{A2} + (Z_{SS}+Z_{RM})*I_{B1} + (Z_{SS}+Z_{LS}+Z_{RS})*I_{B2} + (Z_{SM}+Z_{RS})*I_{C1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{C2} = E_{SB}-E_{RC}$$

$$(Z_{SM}+Z_{RM})*I_{A1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{A2} + (Z_{SM}+Z_{RS})*I_{B1} + (Z_{SM}+Z_{LM}+Z_{RM})*I_{B2} + (Z_{SS}+Z_{RM})*I_{C1} + (Z_{SS}+Z_{LS}+Z_{RS})*I_{C2} = E_{SC}-E_{RB}$$

$$(Z_{SM}+Z_{TM}+Z_{RM})*I_{A1} + (Z_{SM}+Z_{RM})*I_{A2} + (Z_{SM}+Z_{TM}+Z_{RM})*I_{B1} + (Z_{SM}+Z_{RS})*I_{B2} + (Z_{SS}+Z_{TS}+Z_{RS})*I_{C1} + (Z_{SS}+Z_{RM})*I_{C2} = E_{SC}-E_{RC}$$

# Sample Calculation

$$E_{SA} = 1.025 * 138kV / \sqrt{3} \angle 0^\circ$$

$$E_{SB} = 1.025 * 138kV / \sqrt{3} \angle -120^\circ$$

$$E_{SC} = 1.025 * 138kV / \sqrt{3} \angle 120^\circ$$

$$E_{RA} = 1.025 * 138kV / \sqrt{3} \angle 0^\circ$$

$$E_{RB} = 1.025 * 138kV / \sqrt{3} \angle -120^\circ$$

$$E_{RC} = 1.025 * 138kV / \sqrt{3} \angle 120^\circ$$

$$Z_{SS} = 25.15\Omega \angle 86.04^\circ, Z_{SM} = 4.62\Omega \angle -94.67^\circ$$

$$Z_{RS} = 1.91\Omega \angle 85.96^\circ, Z_{RM} = 0.12\Omega \angle -93.10^\circ$$

$$Z_{LS} = 3.05\Omega \angle 77.79^\circ, Z_{LM} = 1.37\Omega \angle 72.62^\circ$$

$$Z_{TS} = 25.47\Omega \angle 74.69^\circ, Z_{TM} = 12.57\Omega \angle 68.25^\circ$$

# Sample Calculation (Cont'd)

Given

Ia1 := 0  
 Ia2 := 0  
 Ib1 := 0  
 Ib2 := 0  
 Ic1 := 0  
 Ic2 := 0

$$(52.28e^{1.406i}) \cdot Ia1 + (27.06e^{1.502i}) \cdot Ia2 + (8.16e^{1.019i}) \cdot Ib1 + (4.74e^{4.632i}) \cdot Ib2 + (8.16e^{1.019i}) \cdot Ic1 + (4.74e^{4.632i}) \cdot Ic2 = 0$$

$$(27.06e^{1.502i}) \cdot Ia1 + (30.08e^{1.487i}) \cdot Ia2 + (4.74e^{4.632i}) \cdot Ib1 + (3.42e^{4.720i}) \cdot Ib2 + (4.74e^{4.632i}) \cdot Ic1 + (3.42e^{4.720i}) \cdot Ic2 = 0$$

$$(8.16e^{1.019i}) \cdot Ia1 + (4.74e^{4.632i}) \cdot Ia2 + (52.28e^{1.406i}) \cdot Ib1 + (25.03e^{1.502i}) \cdot Ib2 + (8.16e^{1.019i}) \cdot Ic1 + (2.71e^{4.623i}) \cdot Ic2 = 0$$

$$(4.74e^{4.632i}) \cdot Ia1 + (3.42e^{4.720i}) \cdot Ia2 + (25.03e^{1.502i}) \cdot Ib1 + (30.08e^{1.487i}) \cdot Ib2 + (2.71e^{4.623i}) \cdot Ic1 + (3.42e^{4.720i}) \cdot Ic2 = 141450e^{4.712i}$$

$$(4.74e^{4.632i}) \cdot Ia1 + (3.42e^{4.720i}) \cdot Ia2 + (2.71e^{4.623i}) \cdot Ib1 + (3.42e^{4.720i}) \cdot Ib2 + (25.03e^{1.502i}) \cdot Ic1 + (30.08e^{1.487i}) \cdot Ic2 = 141450e^{1.571i}$$

$$(8.16e^{1.019i}) \cdot Ia1 + (4.74e^{4.632i}) \cdot Ia2 + (8.16e^{1.019i}) \cdot Ib1 + (2.71e^{4.623i}) \cdot Ib2 + (52.28e^{1.406i}) \cdot Ic1 + (25.03e^{1.502i}) \cdot Ic2 = 0$$

Calculation  
 in Mathcad

Find(Ia1, Ia2, Ib1, Ib2, Ic1, Ic2) =

$$\begin{pmatrix} -0.153 + 1.426i \\ 0.095 - 1.067i \\ 5.313 \times 10^3 + 693.172i \\ -8.611 \times 10^3 - 902.537i \\ -5.312 \times 10^3 - 695.677i \\ 8.61 \times 10^3 + 907.982i \end{pmatrix}$$



# Compare: Analysis vs. Measurements

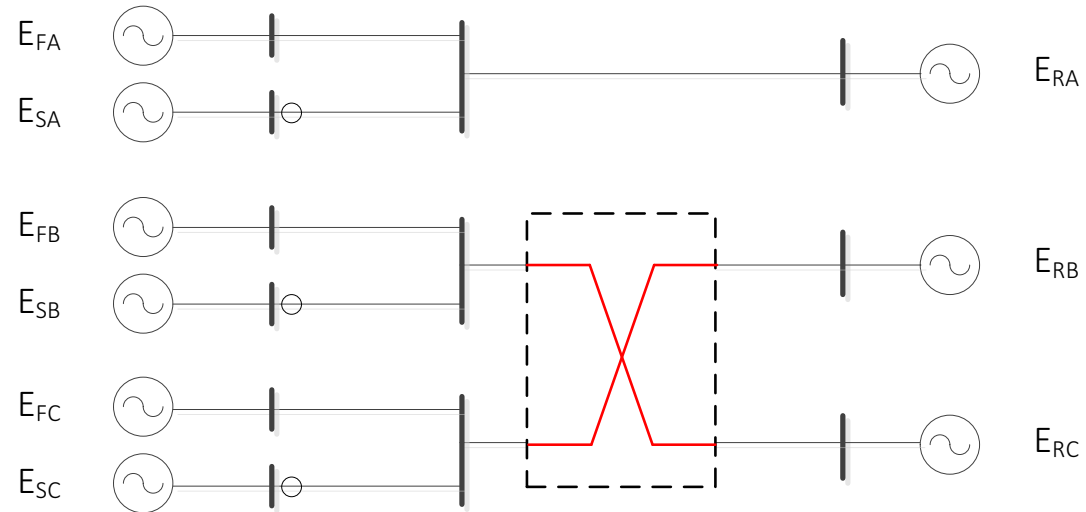
Calculation  
Results

	Complex-Phasor Conversion	
<b>Phase B</b>	-8611-903i	8658.2 ∠ 185.99
<b>Phase C</b>	8610+908i	8657.7 ∠ 6.02

	Measured (A)	Calculated (A)	Error	Error%
<b>Phase B</b>	7723.9 ∠ 290.9°	8658.2 ∠ 185.99°	934.3	<b>10.8</b>
<b>Phase C</b>	7618.0 ∠ 111.9°	8657.7 ∠ 6.02°	1039.7	<b>12</b>
<b>Phasor Shift</b>	179.0°	179.97°	0.97°	<b>0.97°</b>

# Further Discussion

- ▶ In case of cross feeding, current distribution may necessary.



# Further Discussion (Cont'd)

- ▶ What matters: Security Vs. Dependability
  - ❖ In case of phase rolling, the relays need to isolate the phase rolling line as soon as possible
  - ❖ The apparent impedance need to be able to operate the zone 1 or zone 2 distance element of the phase rolling line

# Conclusion

- ▶ Phase rolling is a rare phenomenon.
- ▶ Phasing verification or special synchronizing scheme could be used to prevent from the phase rolling.
- ▶ Phase rolling currents/voltages could be solved electric circuits fundamental knowledges.
- ▶ Apparent impedances could be calculated to verify the possible mis-operation of the non-phase rolling lines or to confirm the relays of the phase rolling lines will operate to isolate.

# Questions

